

**Exercise 1. Impulse**

Consider a bar of radius  $r$  and length  $L$  oriented lengthwise along the  $x$  axis.

**1.1. Suppose  $r=0$**

- (a) If we poke the bar at  $L/2$  with an impulse  $F\Delta t$  compute  $v$
- (b) If we poke the bar at  $L$  with an impulse  $F\Delta t$  compute  $v$

**1.2. Suppose  $r$  is non zero.**

- (a) If we poke the bar at  $L/2$  with an impulse  $F\Delta t$  compute  $v$
- (b) If we poke the bar at  $L$  with an impulse  $F\Delta t$  compute  $v$

**Exercise 2. Virial Theorem**

Suppose that we have a gravitationally bound system that consists of  $N$  individual objects (stars, galaxies, globular clusters, etc.) that have the same mass  $m$  and an average velocity  $\bar{v}$ . Additionally we can measure the dispersion of this velocity  $\sigma$  defined as  $\sigma = \overline{v^2} - \bar{v}^2$

- (a) Use the virial theorem to estimate the total mass of the system
- (b) Suppose a system has a total extent of  $R = 2 \times 10^{18}$  km and a velocity dispersion of 160 km/s. Derive the total mass of the system.
- (c) A respected astronomer measured the visible mass of the system to be  $\approx 10^{10} M_{\odot}$  or  $\approx 2 \times 10^{40}$  kg. Why is there a discrepancy with your derivation?

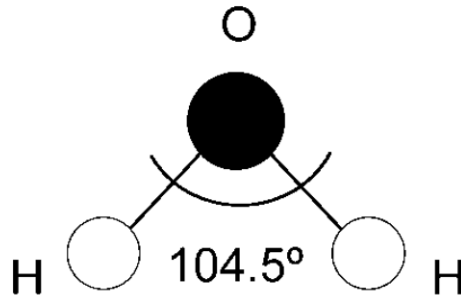
**Exercise 3. Work-Energy Theorem**



Compute the final velocity of the block above. Assume the block slides with no friction.

**Exercise 4. *Moment of Inertia***

The water molecule,  $H_2O$ , is composed of 2 atoms of hydrogen each bonded to one atom of oxygen in a triangular arrangement. The oxygen-hydrogen bonds have a length  $r = 9.6 \times 10^{-11} \text{m}$  and are set apart by an angle of  $104.5^\circ$ . Treat each atom as a point mass.



- (a) Determine the center of mass position of the water molecule
- (b) Find the principal axes that pass through this center of mass
- (c) Confirm these axes by calculating the moment of inertia tensor in the principal axes frame.  
You can write your answer in terms of bond length  $r$  and hydrogen mass  $m_H$