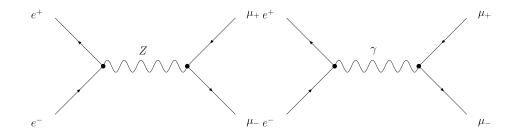
Particle Physics Phenomenology II

FS 11, Series 5

Due date: 28.03.2011, 1 pm

Exercise 1 $e^+e^- \rightarrow \mu^+\mu^-$ with the Z-boson revisited

In the electroweak standard model, the following two diagrams contribute to $e^+e^- \rightarrow \mu^+\mu^$ at tree level:



Use your results of **Series 1** to compute the forward-backward asymmetry for this process for $m_{\mu}^2 \ll s$. Take into account the fact that the Z-boson is unstable, therefore $p^2 - M_Z^2 \rightarrow p^2 - M_Z^2 + iM_Z\Gamma_Z$ in the propagator of the Z-boson. Proceed as follows:

i) Write the differential cross section $\frac{d\sigma}{d\Omega}$ as

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} = \frac{\alpha^2}{4s} \left[A_0 \left(1 + \cos^2 \Theta \right) + A_1 \cos \theta \right].$$

ii) Show that the forward-backward asymmetry is given by

$$A = \frac{F - B}{F + B} = \frac{3A_1}{8A_0}$$

where

$$F = \int_{\cos\theta=0}^{\cos\theta=1} \frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} \mathrm{d}\Omega, \qquad B = \int_{\cos\theta=-1}^{\cos\theta=0} \frac{\mathrm{d}\sigma}{\mathrm{d}\Omega} \mathrm{d}\Omega.$$